

Algebra 1 & Geometry 1

Core Problems — Self-Study Worksheet

ALGEBRA 1

Q01 · Linear Equations — Solving Multi-Step Equations

■ Key: ISOLATE → COMBINE → DIVIDE | Move variable to one side, constants to the other

Solve for x: $5x - 3 = 2x + 12$

(Hint: move x terms to one side first)

x = _____

Q02 · Inequalities — Solving Linear Inequalities

■ Key: FLIP the inequality sign when multiplying/dividing by a NEGATIVE number

Solve for x: $-4x + 1 \geq 13$

Answer: _____

Q03 · Slope & Lines — Slope-Intercept Form

■ Key: $y = mx + b$ | $m = \text{slope (rise/run)}$ | $b = \text{y-intercept}$

A line passes through (2, 1) and (6, 9). What is the slope?

m = _____

Q04 · Systems of Equations — Substitution Method

■ Key: SUBSTITUTE → SOLVE → BACK-SUBSTITUTE

Solve the system:

$$y = 2x - 1$$

$$3x + y = 14$$

What is the value of x?

x = _____

Q05 · Exponents — Laws of Exponents

■ Key: ADD exponents when MULTIPLYING | SUBTRACT when DIVIDING | MULTIPLY when power to a power

Simplify: x^8 / x^3

(Write your answer as x^n — type just the exponent)

$x^{\underline{\hspace{2cm}}}$

Q06 - Factoring — Factoring Trinomials

■ Key: Find two numbers that MULTIPLY to c and ADD to b in x^2+bx+c

Factor completely: $x^2 - 7x + 10$

(Write as $(x - a)(x - b)$, give values of a and b)

$a = \underline{\hspace{1cm}}$, $b = \underline{\hspace{1cm}}$

Q07 - Quadratic Equations — Discriminant & Number of Solutions

■ Key: Discriminant = $b^2 - 4ac$ | > 0 : two roots | $= 0$: one root | < 0 : no real roots

How many REAL solutions does this equation have?

$$2x^2 + 3x + 5 = 0$$

(Answer: 0, 1, or 2)

Number of real solutions: $\underline{\hspace{2cm}}$

Q08 - Functions — Function Notation

■ Key: $f(x)$ means PLUG x in | DOMAIN = all allowed inputs

Given $f(x) = x^2 - 3x + 1$, find $f(4)$.

$f(4) = \underline{\hspace{2cm}}$

Q09 - Percent Change — Calculating Percent Decrease

■ Key: % change = $(\text{new} - \text{old}) / \text{old} \times 100$

A jacket was \$80, now on sale for \$60.

What is the percent decrease? (no % symbol needed)

% decrease = $\underline{\hspace{2cm}}$

Q10 - Word Problems — Setting Up Equations from Context

■ Key: READ → DEFINE variable → TRANSLATE to equation → SOLVE

Maria and Tom together have 35 books.

Maria has 5 more books than Tom.

How many books does Tom have?

Tom = _____

GEOMETRY 1

Q01 - Angles — Complementary & Supplementary Angles

■ Key: Complementary = 90 deg total | Supplementary = 180 deg total

Two supplementary angles: $(3x + 10)$ deg and $(x + 30)$ deg.

Find x.

x = _____

Q02 - Triangles — Triangle Angle Sum

■ Key: ALL triangles sum to 180 deg | Exterior angle = sum of two non-adjacent interior angles

A triangle has angles $2x$ deg, $3x$ deg, and $4x$ deg.

Find x.

x = _____

Q03 - Pythagorean Theorem — Finding the Hypotenuse

■ Key: $a^2 + b^2 = c^2$ | c is ALWAYS the hypotenuse | Triples: 3-4-5, 5-12-13

A right triangle has legs of length 9 and 12.

Find the hypotenuse.

c = _____

Q04 - Area & Perimeter — Area of a Trapezoid

■ Key: $A = \frac{1}{2} \times (b_1 + b_2) \times h$ | b_1, b_2 are the two parallel sides

A trapezoid has bases 8 cm and 14 cm, height 5 cm.

Find the area (in cm^2).

Area = _____ cm^2

Q05 - Circles — Area of a Circle

■ Key: $A = \pi \times r^2$ | $C = 2 \times \pi \times r$ | Always check: radius or DIAMETER?

A circle has a DIAMETER of 12.

What is the area? (Express as multiple of pi)

Area = _____ pi

Q06 - Congruence — Triangle Congruence Theorems

■ Key: SSS / SAS / ASA / AAS / HL | SSA and AAA do NOT prove congruence

Two triangles: two pairs of equal sides,
and the INCLUDED angle (between those sides) is equal.
Which congruence theorem applies?

Theorem: _____

Q07 · Parallel Lines — Angles Formed by a Transversal

■ Key: Alt. Interior = EQUAL | Corresponding = EQUAL | Co-interior = 180 deg

Two parallel lines cut by a transversal.
Co-interior angles: $(2x + 15)$ deg and $(3x + 10)$ deg.

Find x.

x = _____

Q08 · Similar Triangles — Ratios in Similar Figures

■ Key: Similar = same shape, different size | Set up proportion: $a/b = c/d \rightarrow$ cross multiply

Two similar triangles. Smaller triangle has a side of 5;
corresponding side in larger triangle is 20.
Smaller triangle has another side of 9.

Find the corresponding side in the larger triangle.

Side = _____

Q09 · Volume — Volume of a Cone

■ Key: $V(\text{cone}) = 1/3 \times \pi \times r^2 \times h$ | Prism/Cylinder: $V = \text{Base area} \times h$

A cone has base radius 3 and height 7.

Find the volume. (Express as multiple of pi)

V = _____ pi

Q10 · Coordinate Geometry — Distance Formula

■ Key: $d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ | It's Pythagorean theorem on a grid

Find the distance between A(0, 0) and B(6, 8).

d = _____

ANSWER KEY

ALGEBRA 1

#	Answer	Quick Explanation
A01	$x = 5$	
A02	$x \leq -3$	
A03	$m = 2$	
A04	$x = 3$	
A05	x^5	
A06	$a = 2, b = 5 \rightarrow (x-2)(x-5)$	
A07	0 (discriminant = $9-40 = -31 < 0$)	
A08	$f(4) = 5$	
A09	25	
A10	Tom = 15	

GEOMETRY 1

#	Answer	Quick Explanation
G01	$x = 35$	
G02	$x = 20$	
G03	$c = 15$ (9-12-15 = 3x of 3-4-5)	
G04	55 cm ²	
G05	36pi ($r = 6, A = \pi(6^2) = 36\pi$)	
G06	SAS	
G07	$x = 31$	
G08	36 (scale factor = $20/5 = 4$, so $9 \times 4 = 36$)	
G09	21pi ($V = 1/3 \times \pi \times 9 \times 7 = 21\pi$)	
G10	$d = 10$ ($\sqrt{36+64} = \sqrt{100} = 10$)	